## Question 13

Miriam is trying to find the volume of the water tank shown in the photograph on the right.

She takes some measurements and draws a diagram. Part of her diagram is shown below.



Diagram

(a) Using the diagram, find the value of x. Give your answer in metres, correct to two decimal places.



Source: www.watertowersofireland.com. Altered.

$$\frac{x}{20} = \tan 30^{\circ} \implies x = 11.547 = 11.55 \text{ m} (2 \text{ decimal places})$$

(b) The angle of elevation to the bottom of the water tank is  $30^\circ$ , as shown in the diagram. The angle of elevation to the top of the water tank is  $38^\circ$ . Find the distance marked *h* on the photograph. Give your answer correct to one decimal place.



(c) Hugh is also trying to find the volume of the water tank. He estimates that the height, h, is 4.5 m.

By taking **measurements** from the photograph and performing **calculations**, use Hugh's value of h to estimate the volume of the water tank as accurately as you can.

Give your answer correct to the nearest m<sup>3</sup>. State clearly what shape you are taking the water tank to be.

Shape of water tank:	
Cylinder	[Step 1]
Measurements from photograph (label each measurement):	
Diameter = $5.2 \text{ cm}$ [ $\Rightarrow$ Radius =	2.6 cm ]
Height = $2 \cdot 2$ cm	[Step 2]
Calculations: $\frac{\text{Actual radius}}{2 \cdot 6} = \frac{4 \cdot 5}{2 \cdot 2} \implies \text{Actual radius} = 5 \cdot 318 \text{ m}$	[Step 3]
Volume of cylinder = $\pi \times r^2 \times h$ = $\pi \times (5.318)^2 \times 4.5$	[Step 4]
= 399.81	[Step 5]
Volume of water tank, in m <sup>3</sup> : 400 m <sup>3</sup> (nearest m <sup>3</sup> )	